

to 25, without any remainder, then the Author has
the Circle: but this his first Postulatum wants proving.

THE CIRCLE

S Q U A R ' D :

O R,

AN EASY, EXACT, PLAIN and COMPENDIOUS

METHOD of Finding

THE

Exact *Areas* of all *Circles*,

A N D

CIRCULAR BODIES,

By MEANS of the
Due Proportion of the *Diameter* of a Circle
to its *Circumference*; and the *Square Root*
extracted without any *Remainder*.

Never heretofore Published.

By THOMAS BAXTER,
Master of a Private School at CRATHORN,
Cleaveland, YORKSHIRE.


L O N D O N :

Printed for A. BETTESWORTH and C. HITCH,
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and R. AUSTIN, of *Ripon* and *Knaresbrough*.
M D C C X X I I . [Price 1 s. 6 d.]





T H E
P R E F A C E.

 T would be needless, in an Age so capable of *Discerning*, to say any thing of a Work of this Nature, which carries its own *Evidence* at first Sight along with it, did not *Custom* determine in Favour of a *Preface*, and the *Novelty* of the

A 2 Pro-

Project render it somewhat necessary. I understand that some *Criticks* have already past their Verdict upon this Book, affirming, that it were better obliterated, than published : *Because*, say they, many eminent learned Men have laboured very much, in order to find out the due Proportion of the Diameter of a Circle to the Circumference; but it was never yet exactly found; therefore believe it impossible. To whom I answer, That their Assertion is frivolous, and the Reasons thereof ridiculous : For, had never any Age made an Improvement in Learning, then the
Present

Present Age must have known no more than those who lived a thousand Years ago. Do not these *Censorious Criticks* know, that *Truth*, tho' comely in it self, is yet more lovely, when compared with *Falsehood*? How should we know the Excellency of *Light*, if there were no *Darkness*? The *Deficiency*, or *Fallacy*, of the *Proportions* (heretofore published) of a *Circle*, is an *Obscure Mystery* (as I apprehend) to the Majority of *Geometricians*, who assert, *The Area and the Side of the Square Equal of a Circle, may be found, to the ten thousand Part of Unity.* If there were no *Deficiency*

ency or *Fallacy* in their *Principals* or *Base Numbers*, I wou'd acquiesce with those *Affertors* ; but they have not yet founded the Intricacy, therefore they have not found out the Riddle. If the *Proportions* were more contiguous, the *Principals* or *Base Numbers* wou'd be less ; consequently, the *Areas* of all *Circles* would be less ; *et vice versa*, if the *Proportions* were more remote : Notwithstanding the *Square Root* might be as nearly extracted as at present ; as may the *Root* of any *Irrational* or *Surd Number*.

But

But I will let these Men see the Ends for which I have undertaken this Task ; and shall prove the Truth of it even to Demonstration. That a *Square* and a *Circle* may be commensurable, none but a Person divested of Reason and Sense will deny : Because it is obvious to every rational Person, *That two Bodies of different Forms may be of one Magnitude.* Consequently, a *Square* and a *Circle* may be of one *Magnitude.* If a *Square* and a *Circle* may be commensurable ; from hence it must follow, *That a Square may be equal to any Circle of what Magnitude soever.*

Now,

Now, suppose a *Square* and a *Circle* to be commensurable; then an *Irrational* or *Surd* Number, whose *Root* cannot be expressed in *Rational Numbers*, because there is no *Proportion* yet found between an *Irrational* or *Surd* Number and its *Root* : I say, An *Irrational* or *Surd* Number cannot be brought exactly into a *Square*, for the *Reason* above given ; therefore an *Irrational* or *Surd* Number cannot be brought exactly into a *Circle*. If an *Irrational* or *Surd* Number could be exactly brought into a *Circle*, whereas it cannot be brought exactly into a *Square* ; then
a

a *Square* and a *Circle* could not be commensurable : But to demonstrate that a *Square* and a *Circle* cannot be commensurable, is impossible.

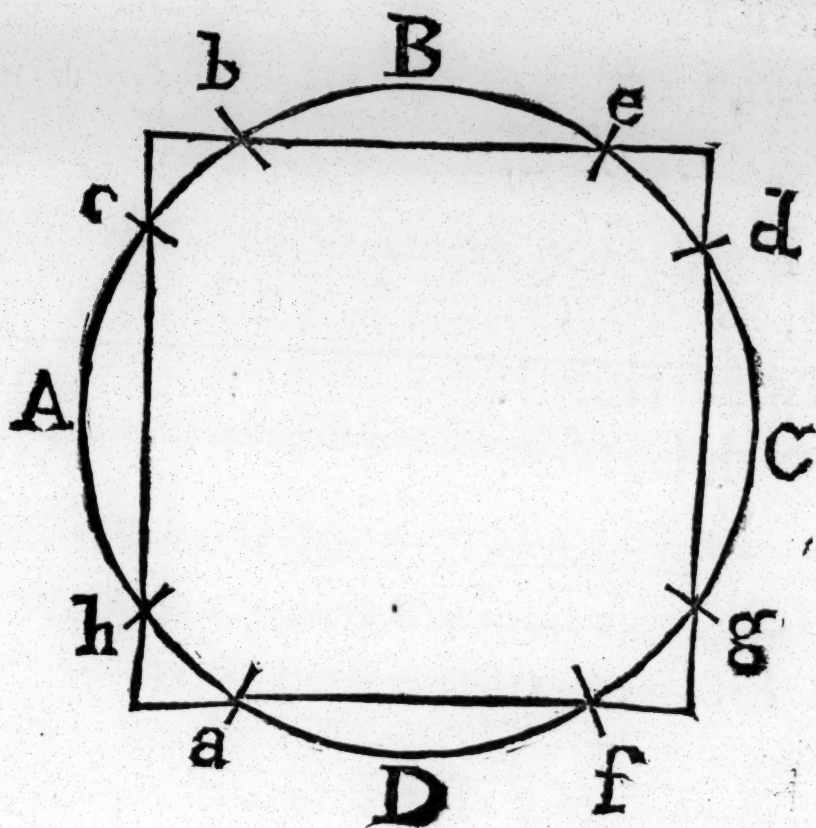
So far as an *Irrational* or *Surd* Number can be brought into a *Square*, so far it may be brought into a *Circle* ; because so far as the *Root* of an *Irrational* or *Surd* Number can be found, so far the *Diameter* of a *Circle* may be found, whose *Area* will be equal to the *Area* of the *Root*. Squaring a *Circle* Geometrically ; that is, with *Rule* and *Compass*, altho' as infallible as any *Rule* in *Geometry*, is now grown obsolete, as I apprehend, because of the

B

Dis-

Discordancy between that and the Numbers. However, as that Difference is now fully reconcil'd, I shall insert the Rule as followeth.

First draw a Circle of any Width or Magnitude ; then divide the Circumference into Four Equal Parts, as A, B, C, D, in this Figure, having your Compass at the same Extent you drew the Circle : Set one Point upon A, with the other bissect the Circumference at a, and b ; do so from B, to c, and d, &c. Lines drawn through these Bissections will produce a Square, equal to the Circle.

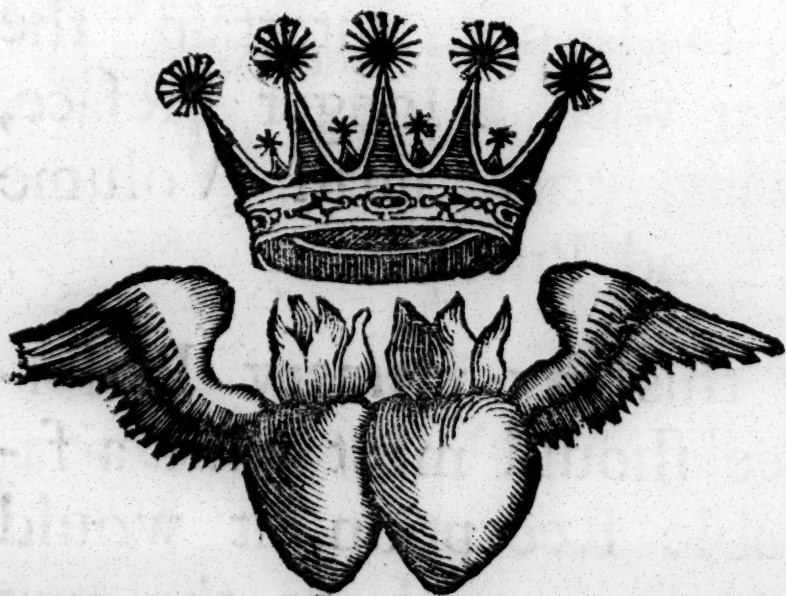


I shall not entertain the Reader with a longer Preface, knowing, this small Volume will stand Proof.

If this my primary Performance should meet with a favourable Reception, it would induce me to enlarge the next

Edition, with Rules for the *Men-
suration* of several *Geometrical Fi-
gures*, or *Bodies* ; which I omit
at present, and conclude, wish-
ing, as no doubt it will, it may
answer the End for which it
was design'd ; that is, be servi-
ceable to the Nation in Ge-
neral. Which is the profound-
est Desires of

Tho. Baxter.



Of

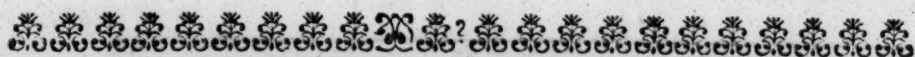


Of a CIRCLE.



CIRCLE is a round Body, or Figure, circumscrib'd within a **LINE**, which is called the *Perephery* or *Circumference*; and the longest Line that can be drawn within a *Circle*, is called the *Diameter*. But I think it needless to dwell upon the Description of the Form or Figure of a Circle; because few *Students in Geometry* are so illiterate, but that they understand the Form and Figure of a *Circle*; and are in greater Want of *Rules*, whereby they may be instructed how to measure a *Circle*, than of the Description of it. Therefore to proceed.

P R O-



P R O B L E M I.

By having the Diameter, to find the Circumference.

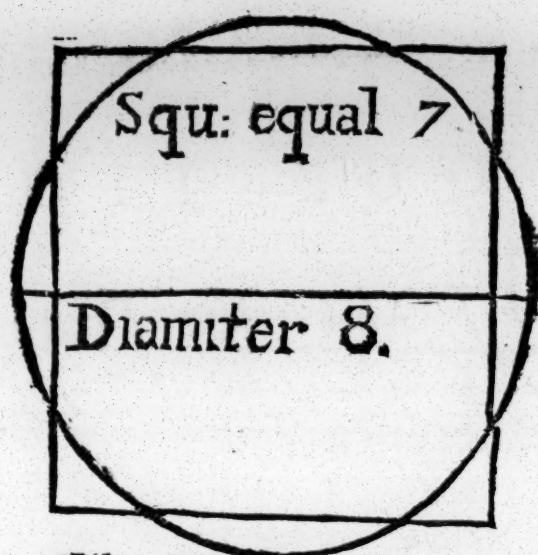
¶ If the *Diameter* of a *Circle* be *Unity*, or *One* ; the *Circumference* of that *Circle* will be 3.0625 ; therefore multiply 3.0625 by the *Diameter* of any *Circle*, the *Product* will be the *Circumference*.

EXAMPLE. Suppose the *Diameter* of a *Circle* be 8, what is the *Circumference*, what is the *Area* ?

Circum. 3.0625 Where the *Diameter* is *Unity*.
Diameter 8

$$\begin{array}{r}
 \hline
 24.5000 \text{ The Length of the Circumference.} \\
 12.25 \\
 4 \\
 \hline
 49.00 \text{ The Area.} \\
 49 \left(7 \text{ The Square Root.} \right. \\
 00
 \end{array}$$

Square



Circumferen: 24.5

Suppose the *Diameter* of a *Circle* be one, the *Square* equal is .875, which being substracted from the *Diameter*, the Remainder is .125 ; which being multiplied by 8, will produce 1 the *Diameter* ; or if it be multiplied by 7, it will produce .875 the Side of the *Square* equal : Which is a Demonstration beyond Contradiction, That if the *Diameter* of a *Circle* be 8, the Side of the *Square* Equal will be 7.



QUESTION.

Q U E S T I O N.

SUPPOSE the Diameter of a CIRCLE be 7.7, what is the Circumference ?

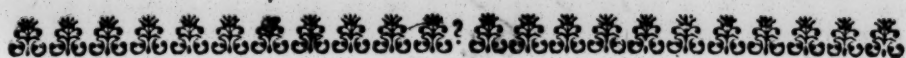
$$\begin{array}{r} 3.0625 \\ 7.7 \\ \hline 214375 \\ 214375 \\ \hline \end{array}$$

23.58125 The *Circumference*.

One Half of which being 11.790625, multiply'd into One Half of 7.7, which is 3.85, the Product will be 45.39390625, the *Area* of that *Circle*, whose *Diameter* is 7.7.



P R O B L E M



P R O B L E M II.

Having the Diameter of a Circle only given, to find the Superficial Content.

If the Diameter of a Circle be One, the Area of that Circle is .765625. Now, as the Square of the Diameter of one Circle is to the Area of that Circle; so is the Square of the Diameter of any other Circle to the Area of that Circle.

Q U E S T I O N.

SUPPOSE the Diameter of a Circle be 8, what is the Area of that Circle? The Square of 8 is 64; and the Square of 1, is 1 : Therefore I multiply 64, the Square of the Diameter, by 765625, the Area of that Circle, whose Diameter is One; and the Product is the Area.

C

765925

[6]

$$\begin{array}{r}
 765625 \\
 64 \\
 \hline
 3062500 \\
 4593750 \\
 \hline
 \end{array}$$

49.000000 The *Area*.

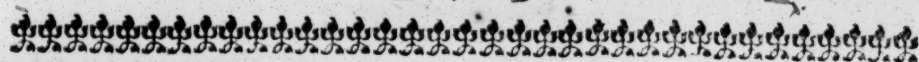
Q U E S T I O N.

SUPPOSE the Diameter of a Circle to be 7.7, what is the Area ?

$$\begin{array}{r}
 7.7 \\
 7.7 \\
 \hline
 539 \\
 539 \\
 \hline
 5929 \\
 765625 \\
 \hline
 29645 \\
 11858 \\
 35574 \\
 29645 \\
 35574 \\
 41503 \\
 \hline
 \end{array}$$

45.39390625 The *Area*.

Q U E.

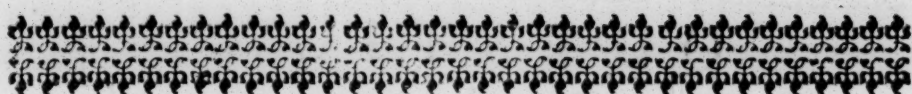


Q U E S T I O N.

SUPPOSE the Diameter of a Circle be $10\frac{2}{7}$, what is the Area?

Now, because there is a *Fraction*, I multiply 10 by 7, adding 2, the *Numerator*, which makes 72 ; which I multiply into itself, and that Product by 765625, then divide this last Product by 49, the *Square* of 7, the *Denominator*, the *Quotient* is the *Area*.

$$\begin{array}{r}
 10\frac{2}{7}) \quad 765625 \\
 \hline
 \quad 5184 \\
 \hline
 72) \quad 3062500 \\
 72) \quad 6125000 \\
 \hline
 144) \quad 765625 \\
 504) \quad 3828125 \\
 5184) \quad 3969000000 \\
 49) \quad 392 \text{ (81 The Area.} \\
 \hline
 \quad 0049 \\
 \quad 49 \\
 \hline
 \quad 00
 \end{array}$$



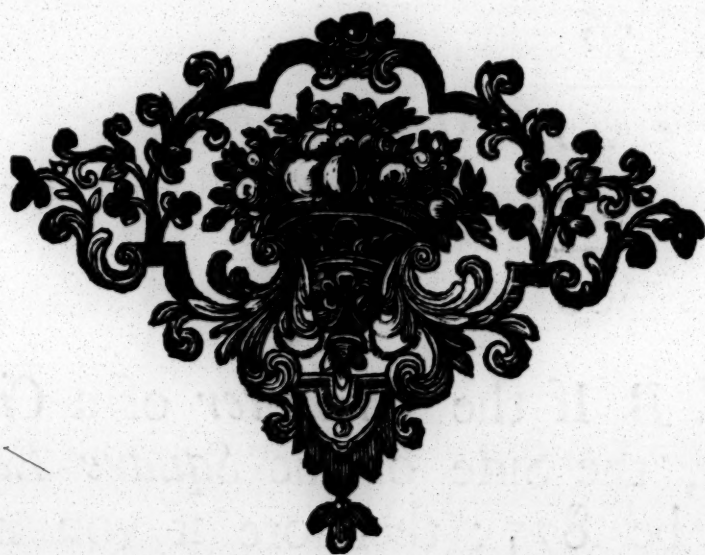
P R O B L E M III.

Having the Diameter, to find the Square Equal.

IF the *Diameter* of a *Circle* be 8, the *Square Equal* will be 7; therefore as 8 is to 7, so is the *Diameter* to the *Square Equal*.

EXAMPLE. Suppose the *Diameter* of a *Circle* be $10\frac{2}{7}$, what is the *Square Equal*? Now, because there is a *Fraction*, I multiply 10, the whole Number, by 7 the *Denominator*, to which I add 2, the *Numerator*, which makes 72, which I multiply by 7, and divide the *Product* by 8, and divide that *Quotient* by 7: This last *Quotient* is the Length of the *Square Equal* to that *Circle* whose *Diameter* is $10\frac{2}{7}$.

$$\begin{array}{r}
 10\frac{1}{2} \\
 \hline
 72 \\
 7 \\
 \hline
 8)504(63, \text{ divide } 63 \text{ the Quotient by} \\
 48 \quad 7, \text{ and the Quotient will be} \\
 \hline
 24 \quad 9, \text{ the Side of the Square} \\
 24 \quad \text{Equal.} \\
 \hline
 00
 \end{array}$$



QUESTION.

SUPPOSE the Diameter of a Circle by 7.7, what is the Side of the Square Equal ?

7.7

$$\begin{array}{r}
 7.7 \\
 \underline{7} \\
 8)539(6.7375 \text{ The Length of the} \\
 \underline{48} \text{Square Equal.} \\
 59 \\
 \underline{56} \\
 30 \\
 \underline{24} \\
 60 \\
 \underline{56} \\
 40 \\
 \underline{40} \\
 00
 \end{array}$$

N. B. If the *Diameter* of a *Circle* be 1, the Side of the *Square Equal* will be .875 ; therefore if you multiply the *Diameter* by .875, the Product will be the Side of the *Square Equal*. This Rule is so plain and obvious, I think it needless to give an Example.

P R O-



P R O B L E M IV.

Having the Square Equal, to find the Diameter.

THIS is but the *Converse* of the last *Problem*: For whereas, in the last *Problem*, you were taught to multiply by 7, and divide by 8 ; here you are to multiply by 8, and divide by 7.

EXAMPLE. The Side of the *Square Equal* of the former *Circle* is 6.7375, what is the *Diameter* ?

As 7 is to 8, so is the Side of the *Square Equal* to the *Diameter*.

$$\begin{array}{r}
 6.7375 \\
 \times 8 \\
 \hline
 7)53.9000 \quad (7.7 \text{ Which is the Length} \\
 \quad 49 \quad \quad \quad \text{of the Diameter.} \\
 \hline
 \quad 49 \\
 \quad 49 \\
 \hline
 \quad 00
 \end{array}$$

Q U E.

Q U E S T I O N.

SUPPOSE the Square Equal be 9, what is the Diameter ?

$$\begin{array}{r}
 9 \\
 8 \\
 \hline
 7 \overline{) 72} \text{ (} 10\frac{2}{7} \text{ The Length of the} \\
 \quad 7 \quad \text{Diameter.} \\
 \hline
 02
 \end{array}$$

To find the *Area*, where the *Diameter* of a *Circle* is $10\frac{2}{7}$; First, multiply 10 the whole Number by 7 the *Denominator* : Add 2, the *Numerator*, which will make the Sum 72 : Multiply 3.0625 by 72, divide the Product by the *Square* of the *Denominator*, viz. 49. Multiply half the *Quotient* by the half of 72, viz. 36, the Product is the *Area* of that *Circle* whose *Diameter* is $10\frac{2}{7}$. Behold the Work!

$10\frac{2}{7}$

$$\begin{array}{r} 10^2 \\ \hline 72 \end{array}$$

$$\begin{array}{r} 3.0625 \\ \hline 72 \end{array}$$

$$61250$$

$$214375$$

$$49 \overline{) 220.5.000} \quad (45$$

$$\underline{196}$$

$$0245$$

$$\underline{245}$$

$$000$$

$$225$$

$$\underline{36}$$

$$1350$$

$$\underline{675}$$

$$81.00$$

Half of the Circumference.

The Area.

P R O B L E M V.

Having the Square Equal, to find the Circumference.

 If the Square Equal be Unity, or One, the Circumference will be 3.5 : Therefore as 1 is to 3.5, so is the Square Equal to the Circumference. As 1 does neither multiply nor divide, hence it follows, That if you multiply the Square Equal by 3.5, the Product will be the Circumference.

Example. If the Side of the Square Equal be 6.7375, what is the Circumference?

$$6.7375$$

$$\underline{3.5}$$

$$336875$$

$$\underline{202125}$$

$$23.58125$$

The Length of the Circumference.

D

Q U E-

Q U E S T I O N.

If the Side of the Square Equal
be 9, what is the Circumference?

$$\begin{array}{r} 3.5 \\ \hline 9 \end{array}$$

31.5 The Length of the Circumference.



P R O B L E M VI.

Having the Circumference, to find the
Diameter.

Multiply the Circumference by
16, divide the Product by 49,
the Quotient is the Diameter.

EXAMPLE. Suppose the Cir-
cumference of a Circle be 23.58125,
what is the Diameter?

$$\begin{array}{r} 23.58125 \\ \times 16 \\ \hline 14148750 \\ 2358125 \\ \hline \end{array}$$

377.30000

49) 377.3 (7.7 The Length of the
Diameter.

$$\begin{array}{r} 343 \\ \hline 343 \\ 343 \\ \hline 000 \end{array}$$

Q U E-

Q U E S T I O N.

IF the Circumference of a Circle be 31.5, what is the Diameter ?

$$\begin{array}{r} 31.5 \\ 16 \\ \hline 1890 \\ 315 \\ \hline \end{array}$$

49) 504.0 ($10\frac{14}{49}$ The Diameter.

$$\begin{array}{r} 49 \\ \hline 014 \end{array}$$

Abbreviate the Fraction, *i. e.* Divide both the *Numerator* and *Denominator* by 7, and you'll have $10\frac{2}{7}$ for the *Diameter*, as in the 4th Problem. The Reader, perhaps, may have some Trouble to find out the Reason of the Discordancy between the *Circumference* here supposed, and the 4th Problem, where the *Diameter* is the same as here. But observe the following Sollution : If I had divided 220.5 by 7, the *Denominator* of the *Fraction*, the *Quotient* would have been 31.5 as above, (which is the exact Circumference) but then I must have divided the last *Product* by 7, to find the *Area*. However, I shall insert the *Question* as followeth, wrought both Ways.

$$\begin{array}{r} 10^2 \\ \hline 72 \end{array}$$

[16]

3.0625

72

61250

214375

49) 220.5000 (4.5

196

2.25

245

36

245

000

1350

675

81.00 The Area.

3.0625

72

61250

214375

7) 220.5000 (31.5

21

15.75

10

36

7

9450

35

4725

35

7) 567.00 (81 Area.

00

56

00

007

N. B. Where a Number is proposed,
that will neither divide exactly by 49,
nor

nor the Fractions by 7, it is *Irrational*; therefore its *Diameter* cannot be exactly found. A *Diameter* may be found, whose Circumference will be as near the proposed Number, as any *Rational* Number can come, or be near, to an *Irrational* Number.

Q U E S T I O N.

SUPPOSE the Circumference of a Circle be 48, what is the Diameter, what is the Area?

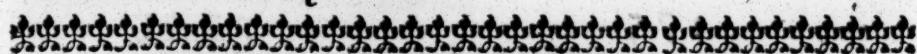
$ \begin{array}{r} 48 \\ 16 \\ \hline 288 \\ 48 \\ \hline 49 \overline{)768} (15.6734 \text{ Dia.} \\ \underline{49} \\ 278 \\ \underline{245} \\ 330 \\ \underline{294} \\ 360 \\ \underline{343} \\ 170 \\ \underline{147} \\ 230 \\ \underline{196} \\ 34 \end{array} $	$ \begin{array}{r} 3.0625 \text{ Circumference} \\ \text{of 1, the Diam.} \\ 156734 \text{ The Diameter.} \\ \hline 122500 \\ 91875 \\ 214375 \\ 183750 \\ 153125 \\ 30625 \\ \hline 47.99978750 \\ 2399989375 \text{ Semicircumfer.} \\ 78367 \text{ Semidiameter.} \\ \hline 16799925625 \\ 14399936250 \\ 7199968125 \\ 19199915000 \\ 16799925625 \\ \hline 188.079967350625 \text{ Area.} \end{array} $
--	---

Whole *Square Root* is 13.714225 :
Which might have been brought nearer the Truth by finding the Diameter to a greater Length. To demonstrate the Matter more fully, behold the following Work.

$ \begin{array}{r} 48, \text{the Circum-} \\ 16 \text{ ference.} \\ \hline 288 \\ 48 \\ \hline 49 \overline{) 768} (15\frac{33}{49} \text{ Dia.} \\ \underline{49} \\ 278 \\ \underline{245} \\ 33 \end{array} $	$ \begin{array}{r} 15\frac{33}{49} \\ 768 \\ 384 \text{ Semidiameter.} \\ 24 \text{ Semicircumference.} \\ \hline 1536 \\ \underline{768} \\ 49 \overline{) 9216} (188\frac{4}{49} \text{ Area.} \\ \underline{49} \\ 431 \\ \underline{392} \\ 396 \\ \underline{392} \\ 4 \end{array} $
---	---

If a *Square* were proposed, whose Side was 13 $\frac{7}{11}$, (or the like) it would be impossible to find the exact *Area*, without *Fractions*, to remain; because it is an *Irrational Number*, notwithstanding an *Irrational Diameter* and *Circumference* must belong to an *Irrational Number*. As no *Number* can be brought into a *Square* but what

what may be brought into a *Circle*, nor no Number can be brought into a *Circle* but what may be brought into a *Square* (by my *Proportions*); it must either be allowed, That *Mine* are *Due Proportions*; or else be demonstrated, That a *Square* and a *Circle* cannot be commensurable; the which is impossible.



P R O B L E M VII.

Having the Circumference, to find the Square Equal.

THIS is the Converse of the Fifth Problem: Whereas multiplying the *Square Equal* by 3.5, found the *Circumference*; it must follow, that Dividing the *Circumference* by 3.5, will find the Side of the *Square Equal*.

EXAMPLE. Suppose the Circumference of a *Circle* be 31.5, what is the Side of the *Square Equal*?

3.5) 315 (9 The Side of the *Square Equal*.
 315

 000

Q U E S T I O N.

SUPPOSE the Circumference of a *CIRCLE* be 3.5)

3.5)23.58.125(6.7375 The Side of the
Square Equal.

$$\begin{array}{r}
 210 \\
 \hline
 258 \\
 245 \\
 \hline
 131 \\
 105 \\
 \hline
 262 \\
 245 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 175 \\
 \hline
 1475 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 000 \\
 \hline
 \end{array}$$

~~~~~

# Q U E S T I O N.

**S**UPPOSE the Circumference be  
245, what is the Square Equal?

3.5) 245 ( 7 The Side of the *Square*  
*Equal.*

$$\begin{array}{r}
 245 \\
 \hline
 000 \\
 \hline
 \end{array}$$

~~~~~

P R O B L E M VIII.

Having the AREA, to find the
Circumference.

AS the Square of the Circumfe-
rence of one Circle, is to the
Area of that Circle; so is the
Square of the Circumference of any
other Circle, to the Area of that
Circle. If

If the Area of a Circle be 1, the Square of the *Circumference* will be 12.25 : Therefore as 1 is to 12.25, so is the Area to the *Square* of the *Circumference*.

EXAMPLE. Suppose the Area of a *Circle* be 81, what is the *Circumference* ?

$$\begin{array}{r}
 12.25 \\
 81 \\
 \hline
 1225 \\
 9800 \\
 \hline
 992.25 \cdot (31.5 \text{ The Circumference.} \\
 9 \\
 \hline
 092 \\
 61 \\
 \hline
 3125 \\
 625 \\
 \hline
 3125 \\
 \hline
 0000
 \end{array}$$

Q U E S T I O N.

SUPPOSE the Area of a Circle be 45.39390625, what is the *Circumference* ?

E

45.

[22]

45.39390525

1225

22696953125

9078781250

9078781250

4539390625

5560753515625

556.07.53.51.56.25. (23.58125 The
4 Circumference.

156

43

129

2707

465

2325

38253

4708

37664

58951

47161

1179056

471622

943244

23581225

4716245

23581225

00000000

P R O-

P R O B L E M IX.

Having the Area, to find the Diameter.

 M Multiply the *Area* by 64, extract
 the Square Root of that Pro-

 duct, divide the *Root* by 7, the
Quotient is the *Diameter*.

EXAMPLE. Suppose the *Area*
 of a *Circle* be 45.39390625, what is
 the *Diameter* ?

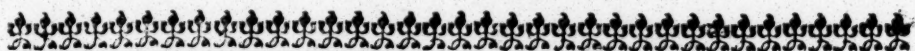
45.39390625 <div style="text-align: right; margin-right: 20px;">64</div> <hr style="width: 100%;"/> 18157562500 27236343750 <hr style="width: 100%;"/> 290521000000	Root. 7(539(7.7 The 49 <i>Diameter</i> . <hr style="width: 50%;"/> 49 <hr style="width: 50%;"/> 49 <hr style="width: 50%;"/> 00
25 <hr style="width: 50%;"/> 405 103 309 <hr style="width: 50%;"/> 9621 1069 9621 <hr style="width: 50%;"/> 0000	

Q U E S T I O N.

SUPPOSE the *Area* of a *Circle*
 be 81, what is the *Diameter* ?

$$\begin{array}{r}
 81 \\
 64 \\
 \hline
 324 \\
 486 \\
 \hline
 5184 \\
 49 \\
 \hline
 284 \\
 142 \\
 \hline
 284 \\
 \hline
 000
 \end{array}$$

$$\begin{array}{r}
 \text{Root.} \\
 (7 (72 (10 \frac{2}{7} \text{ The Dia-} \\
 \quad \quad \quad 7 \quad \quad \quad \text{meter.} \\
 \hline
 02
 \end{array}$$



P R O B L E M X.

Having the Circumference, to find the Area.

*** This is Converse of the 8th Problem. If the Square of the Circumference of a Circle be 1225, the Area is 1 : Therefore as 12.25 is to 1, so is the Square of the Circumference of any Circle to its Area.

EXAMPLE. Suppose the Circumference be 23.58125, what is the Area ?

[25]

23.58125

23.58125

11790625

4716250

2358125

18865000

11790625

7074375

4716250

12.25) 556075.3515625 (45.39390625

4900

6607

6125

4825

3675

11503

11025

4785

3675

11101

11025

7656

7350

3062

2450

6125

6125

0000

The *Area*.

Q U E

Q U E S T I O N.

SUPPOSE *the* Circumference be 31.5, *what is the* Area ?

315

315

315

575

945

1225) 99225 (81 The *Area*.

9800

1225

1225

0000

I shall so far oblige the Curious, as to give Rules for finding the Side of the Square *Inscrib'd*, and the Side of the Square *Inscribing*, tho' not exactly ; because it is impossible to find the *Hypothenusal* or *Subtending* Line (*exactly*) of a *Right Angled Triangle*, when the Sum or Length of the Legs are equal. Neither has it any Relation to the finding the just *Area* of a *Circle*.

P R O-

P R O B L E M XI.

Having the Diameter, to find the Side of the Square Inscrib'd.

* I *
* * *
F the *Diameter* of a *Circle* be 1, the *Side* of the *Square Inscrib'd* will be 707107: Therefore as 1 is to 707107, so is the *Diameter* to the *Square Inscrib'd*.

EXAMPLE. If the *Diameter* of a *Circle* be 7.7, what is the *Side* of the *Square Inscrib'd*?

$$\begin{array}{r} 707107 \\ 77 \\ \hline 4949749 \\ 4949749 \\ \hline \end{array}$$

5.4447239 The *Side* of the *Square Inscrib'd*.

P R O B L E M XII.

Having the Circumference, to find the Side of the Square Inscrib'd.

* I *
* * *
F the *Circumference* be 1, the *Side* of the *Square Inscrib'd* will be 230892: Therefore as 1 is to 230892, so is the *Circumference* to the *Square Inscrib'd*. Q U E-

Q U E S T I O N.

I*F the Circumference of a Circle be 2358125, what is the Square Inscrib'd ?*

$$\begin{array}{r}
 230892 \\
 \hline
 4716150 \\
 21223125 \\
 18865000 \\
 7074375 \\
 4716150 \\
 \hline
 \hline
 \end{array}$$

5.44472197500 The Side of the *Square Inscrib'd.*

P R O B L E M XIII.

Having the Side of the Square Equal, to find the Side of the Square Inscrib'd.

*****I******F the Side of Square Equal be 1, the Side of the Square Inscrib'd will be 808122 : Therefore as 1 is to 808122, so is the Side of the Square Equal to a Circle, to the Side of the Square Inscrib'd within a Circle.*

EXAMPLE.

EXAMPLE. If the Side of the Square Equal of a Circle be 6.7375, what is the Side of the Square In-
scrib'd ?

$$\begin{array}{r}
 6.7375, \\
 808122 \\
 \hline
 134750 \\
 134750 \\
 67375 \\
 539000 \\
 539000 \\
 \hline
 \hline
 \hline
 \end{array}$$

5.4447219750 The Side of the Square Inscrib'd.

~~~~~

# P R O B L E M XIV.

*Having the Side of a Square, to find the Diameter of a Circle, that will circumscribe that Square.*

\*\*\*:\*\*\* F the Side of a Square be 1,  
 \*\*\* I \*\*\* the Diameter of a Circle to cir-  
 \*\*\* cumscribe that Square will be  
 1.4142 : Therefore as 1 is to 1.4142,  
 so is the Side of a Square to the Dia-  
 meter of a Circle that will circumscribe  
 that Square.

F

EXAM-



*EXAMPLE.* Suppose the Side of a *Square* be 5.444721975, what is the *Diameter* of a *Circle* that will circumscribe that *Square* ? Behold the Work as followeth.

$$\begin{array}{r}
 5.444721975 \\
 \quad 1.4142 \\
 \hline
 10889443950 \\
 21778887900 \\
 \hline
 5444721975 \\
 21778887900 \\
 \hline
 5444721975 \\
 \hline
 76.99925817045 \text{ The Length of the } \textit{Diameter}.
 \end{array}$$

~~~~~

To find the Area of a Semicircle.

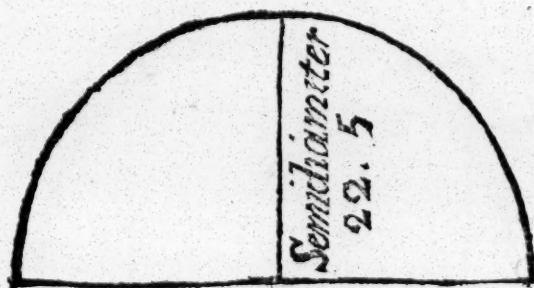
~~~~~ T may be performed two Ways.  
 I i. e. You may either find the *Area* of the whole *Circle*, as hath been already taught,  $\frac{1}{2}$  of which is the *Area* of the *Semicircle* : Or multiply 3.0625 by the *Semidiameter*,  $\frac{1}{2}$  of that Product multiplied by the *Semidiameter* is the *Area*.

*EXAM.*

[ 31 ]

*EXAMPLE.* Suppose the *Semi-diameter* be 22.5, what is the *Area*?

$$\begin{array}{r}
 3.0625 \\
 22.5 \\
 \hline
 153125 \\
 61250 \\
 61250 \\
 \hline
 6890625 \\
 34453125 \\
 225 \\
 \hline
 172265625 \\
 68906250 \\
 68906250 \\
 \hline
 775.1953125 \text{ The Area.}
 \end{array}$$



I shall omit giving an Example the other Way, because it differs nothing

thing from what has been spoken, of the *Menfuration of Circles*, save dividing the Product by 2, the Quotient is the *Area* of a *Semicircle*.

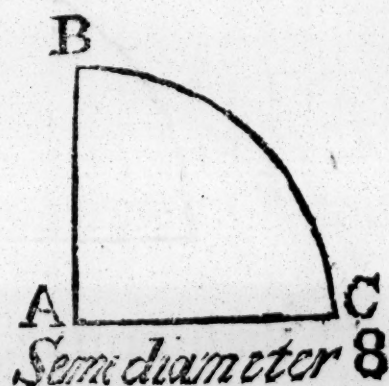
Of a QUADRANT.

THE *Area* of a *Quadrant*, or fourth Part of a *Circle*, may be thus found.

Multiply 1.53125 by the *Semidiameter*, divide the Product by 2, multiply the Quotient by your former Multiplier : This last Product is the *Area* of the *Quadrant*.

EXAMPLE. Let *A, B, C*, be a *Quadrant*, or fourth Part of a *Circle*, whose *Radius* or *Semidiameter* is 8; what is the *Area* ?

$$\begin{array}{r}
 1.53125 \\
 \times 8 \\
 \hline
 1225000 \\
 612500 \\
 \hline
 8 \\
 \hline
 49.00000 \text{ The Area.}
 \end{array}$$



Of



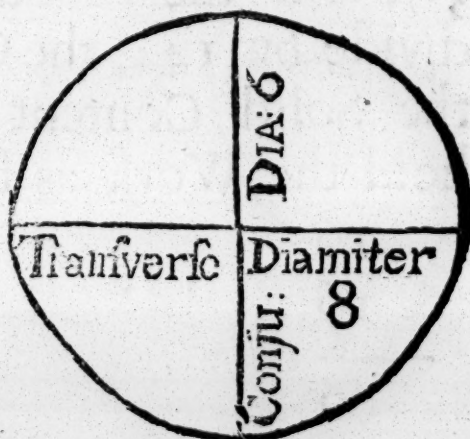
\*\*\*\*\*

# *Of an ELLIPSIS.*

**A**N *Ellipsis*, or *Oval*, is a Figure bounded by a *Regular Curve Line* returning into itself; but of its two *Diameters* cutting each other in the *Centre*, one is longer than the other, in which it differs from the *Circle*. To find the *Area* this is the Rule : Multiply the *Transverse Diameter* by the *Conjugate* : Multiply that Product by 765625. This last Product is the *Area* of the *Ellipsis*, or *Oval*.


**EXAMPLE.** If the *Transverse Diameter* of an *Oval* be 8, and the *Conjugate Diameter* 6, what is the *Area* ?

$$\begin{array}{r}
 8 \quad 765625 \\
 6 \quad \quad 48 \\
 \hline
 48 \quad 6125000 \\
 \quad 3062500 \\
 \hline
 36.750000 \text{ Area.}
 \end{array}$$



*Of*

## Of a C O N E.

 *Cone* is a Solid, having a *Circular Base*, and growing smaller and smaller, till it ends in a Point, which is called the *Vertex*, and may be nearly represented by a *Sugar Loaf*. To find the Solidity, this is the Rule : Multiply the *Area* of the *Base* by a third Part of the *Perpendicular Height*, the Product is the Solid Content. Thus let *A, B, C*, be a *Cone*, the *Diameter* of whose Base *A, B*, is 16 Inches, and the Height of the Cone *D, C*, is 10½ Feet : First, Square the *Diameter* 16, and it is 256 ; which multiply by 765625, and the Product is 196 ; which multiply by a third Part of the Height, viz. 3.5, and the Product is 686 ; which divide by 144, the Quotient is 4.763<sup>8</sup>, the Solid Content of the *Cone*. Behold the Work as below.

$$\begin{array}{r}
 16 \\
 16 \\
 \hline
 96 \\
 16 \\
 \hline
 \end{array}$$

256 Square of the *Diameter*.

[ 35 ]

765625  
 256

4593750  
 3828125  
 1531250

196.000000 Area of the *Base*.

3.5 A third Part of the *Height*.

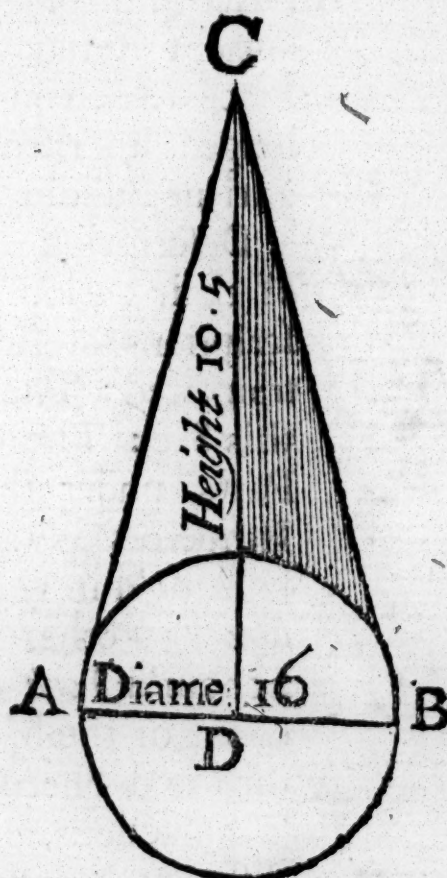
980  
 588

144)686.0(4.763<sup>8</sup> } The Con-  
 576 } tent of  
           } the Cone.

1100  
 1008

920  
 864

560  
 432  
 128



**F I N I S.**



~~~~~  
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7

2

4

1

1

9